

If  $a, b, c, d$  are four distinct positive quantities in G.P., then show that

$$a + d > b + c$$

**SOLUTION :**

**AM > GM** [because all terms are distinct the equality in the AM,GM inequality holds when all terms involved in the mean are equal but in the question, it's mentioned that  $a, b, c, d$  are different]

$a, b, c, d$  are in G.P

$$b = \sqrt{ac}$$

$$c = \sqrt{bd}$$

now,

$$\begin{aligned} a + c &> 2\sqrt{ac} > \cancel{2b} \\ &> 2b \quad - \textcircled{1} \end{aligned}$$

$$\begin{aligned} b + d &> 2\sqrt{bd} \\ &> 2c \quad - \textcircled{2} \end{aligned}$$

add  $\textcircled{1}$  &  $\textcircled{2}$

$$(a + c) + (b + d) > 2b + 2c$$

$$\Rightarrow a + d > b + c$$

hence proved