

## L'Hopital's Rule

It is applicable while calculating limits of indeterminate forms of the type  $\frac{0}{0}$ ,  $\frac{\infty}{\infty}$ . If the functions  $f(x)$  &  $g(x)$  are differentiable in certain neighbourhood of a point  $a$ , except, maybe, at the point  $a$  itself, &  $g'(x) \neq 0$  and if

$$\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} g(x) = 0$$

or

$$\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} g(x) = \infty$$

then

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$$

provided the limit  $\lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$  exists.

Indeterminate forms of the type  $0 \cdot \infty$  or  $\infty - \infty$  are reduced to forms of type  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$  by algebraic transformation.

Indeterminate forms of the type  $1^\infty$ ,  $\infty^\infty$ ,  $\infty \cdot 0^\infty$  are reduced to forms of the type  $0 \cdot \infty$  by taking logarithms or by transformation

$$[f(x)]^{\phi(x)} = e^{\phi(x) \cdot \ln f(x)}$$