

Evaluate the value of $\lim_{x \rightarrow 0} \frac{\sin x}{x}$ using series expansion

SOLUTION :

swe know that

$$\sin x = \frac{x^1}{1!} - \frac{x^3}{3!} + \frac{x^5}{5!} \dots \dots \dots$$

$$\frac{\sin x}{x} = 1 - \frac{x^2}{3!} + \frac{x^4}{5!} \dots \dots \dots$$

$$\begin{aligned} \lim_{x \rightarrow 0} \frac{\sin x}{x} &= \lim_{x \rightarrow 0} \left(1 - \frac{x^2}{3!} + \frac{x^4}{5!} \dots \dots \dots \right) \\ &= 1 \end{aligned}$$

NOTE :

$$\lim_{x \rightarrow 0} x^n = 0 \quad [n > 0]$$