

Q. Q. If  $g(x)$  is a curve which is obtained by the reflection of  $f(x) = \frac{e^x - e^{-x}}{2}$  about the line  $y=x$  then

- A -  $g(x)$  has more than one tangent parallel to  $x$ -axis.
- B -  $g(x)$  has more than one tangent parallel to  $y$ -axis.
- C -  $y=x$  is a tangent to  $f(x)$  at  $(0,0)$ .
- D -  $g(x)$  has no extremum.

Ans: D.

As  $g(x)$  is a curve which is obtained by the reflection of  $f(x) = \frac{e^x - e^{-x}}{2}$  on  $y=x$

$\Rightarrow g(x)$  is inverse of  $f(x)$ .

$$\therefore g(x) = \log(x + \sqrt{x^2 + 1}) = f^{-1}(x)$$

$$\Rightarrow g'(x) = \frac{1}{x + \sqrt{x^2 + 1}} \left( 1 + \frac{2x}{2\sqrt{x^2 + 1}} \right) = \frac{1}{\sqrt{1+x^2}} > 0, \forall x \in \mathbb{R}$$

$\Rightarrow g(x)$  has no tangent parallel to  $x$ -axis also  $g(x)$  is always defined,  $\forall x \in \mathbb{R}$ .

$\Rightarrow g(x)$  has no tangent parallel to  $y$ -axis since  $g'(x) > 0$

$\Rightarrow g(x)$  has not any extremum.