

Exemplar Problem with Solution :

Q) Suppose an integer from 1 through 1000 is chosen at random, find the probability that the integer is a multiple of 2 or a multiple of 9.

Sol: We have integers 1,2, 3,...1000

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$$n(S) = 1000$$

Number of integers which are multiple of 2 = 500 Let the number of integers which are multiple of 9 be n.

$$\text{nth term} = 999 \Rightarrow 9 + (n - 1)9 = 999$$

$$\Rightarrow 9 + 9n - 9 = 999$$

$$\Rightarrow n = 111$$

From 1 to 1000, the number of multiples of 9 is 111.

The multiple of 2 and 9 both are 18, 36,..., 990.

Let m be the number of terms in above series.

$$\therefore \text{mth term} = 990$$

$$\Rightarrow 18 + (m - 1)18 = 990$$

$$\Rightarrow m = 55$$

$$\text{Number of multiples of 2 or 9} = 500 + 111 - 55 = 556 = n(E)$$