

Let $A(1, 1, 1)$, $B(2, 3, 5)$, $C(-1, 0, 2)$ be three points, then equation of a plane parallel to the plane ABC which is at a distance 2 from origin, is

$$\text{(1)} \quad 2x - 3y + z + 2\sqrt{14} = 0$$

$$\text{(2)} \quad 2x - 3y + z - \sqrt{14} = 0$$

$$\text{(3)} \quad 2x - 3y + z + 2 = 0$$

$$\text{(4)} \quad 2x - 3y + z - 2 = 0$$

$$A(1,1,1) \quad B(2,3,5) \quad C(-1,0,2)$$

$$\vec{AB} = (1, 2, 4) \quad \vec{AC} = (-2, -1, 1)$$

Direction ratios of plane ABC

is along $\vec{AB} \times \vec{AC}$

$$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 4 \\ -2 & -1 & 1 \end{vmatrix}$$

$$\hat{i}(6) - \hat{j}(9) + \hat{k}(3)$$

$$\Rightarrow (6, -9, 3) \text{ or } (2, -3, 1)$$

From options only option (1) has distance of 2 from origin and having direction ratios same.