

1. If the letters of the word ALGORITHM are arranged at random in a row what is the probability the letters GOR must remain together as

Given word is ALGORITHM

⇒ Total number of letters in algorithm = 9

∴ Total number of words = 9!

So, $n(S) = 9!$

If 'GOR' remain together, then we consider it as one group.

∴ Number of letters = 7

Number of words, if 'GOR' remain together in the order = 7!

So, $n(E) = 7!$

Required Probability = $\frac{\text{Number of favourable outcome}}{\text{Total number of outcomes}}$

$$= \frac{n(E)}{n(S)}$$

$$= \frac{7!}{9!} [\because n! = n \times (n - 1) \times (n - 2) \dots 1]$$

$$= \frac{7!}{9 \times 8 \times 7!} = \frac{1}{72}$$