Circles - Class XI

Past Year JEE Questions

Questions

Quetion: 01

The locus of a point, which moves such that the sum of squares of its distances from the points (0, 0), (1, 0), (0, 1), (1, 1) is 18 units, is a circle of diameter d. Then d² is equal to ______.

Solutions

Solution: 01

Answer Correct Answer is **16**

Explanation

Let point P(x, y)

A(0, 0), B(1, 0), C(0, 1), D(1, 1)

$$(PA)^{2} + (PB)^{2} + (PC)^{2} + (PD)^{2} = 18$$

$$x^{2} + y^{2} + x^{2} + (y-1)^{2} + (x-1)^{2} + y^{2} + (x-1)^{2} + (y-1)^{2} = 18$$

$$\Rightarrow 4(x^2 + y^2) - 4y - 4x = 14$$

 $\Rightarrow x^2 + y^2 - x - y - \frac{7}{2} = 0$

$$d = 2\sqrt{\frac{1}{4} + \frac{1}{4} + \frac{7}{2}}$$

$$\Rightarrow d^2 = 16$$