

Let $p, q \in \mathbb{R}$. If $2 - \sqrt{3}$ is a root of the quadratic equation, $x^2 + px + q = 0$, then:

$$(1) \quad p^2 - 4q + 12 = 0 \qquad (2) \quad q^2 - 4p - 16 = 0$$

$$(3) \quad q^2 + 4p + 14 = 0 \qquad (4) \quad p^2 - 4q - 12 = 0$$

(4) Since $2 - \sqrt{3}$ is a root of the quadratic equation $x^2 + px + q = 0$

$\therefore 2 + \sqrt{3}$ is the other root

$$\begin{aligned} \Rightarrow x^2 + px + q &= [x - (2 - \sqrt{3})][x - (2 + \sqrt{3})] \\ &= x^2 - (2 + \sqrt{3})x - (2 - \sqrt{3})x + (2^2 - (\sqrt{3})^2) \\ &= x^2 - 4x + 1 \end{aligned}$$

Now, by comparing $p = -4, q = 1$
 $\Rightarrow p^2 - 4q - 12 = 16 - 4 - 12 = 0$