

If  $\alpha$  and  $\beta$  be the roots of the equation  $x^2 - 2x + 2 = 0$ , then

the least value of  $n$  for which  $\left(\frac{\alpha}{\beta}\right)^n = 1$  is :

- (1) 2            (2) 5            (3) 4            (4) 3

(3) The given quadratic equation is  $x^2 - 2x + 2 = 0$

Then, the roots of the this equation are  $\frac{2 \pm \sqrt{-4}}{2} = 1 \pm i$

$$\text{Now, } \frac{\alpha}{\beta} = \frac{1-i}{1+i} = \frac{(1-i)^2}{1-i^2} = i$$

$$\text{or } \frac{\alpha}{\beta} = \frac{1-i}{1+i} = \frac{(1-i)^2}{1-i^2} = i$$

$$\text{So, } \frac{\alpha}{\beta} = \pm i$$

$$\text{Now, } \left(\frac{\alpha}{\beta}\right)^n = 1 \Rightarrow (\pm i)^n = 1$$

$\Rightarrow n$  must be a multiple of 4.

Hence, the required least value of  $n = 4$ .