

Question 8: If $2+i\sqrt{3}$ is a root of the equation $x^2 + px + q = 0$, where p and q are real, then (p, q) equals

(a) $(-4, 7)$

(b) $(4, -7)$

(c) $(-7, 4)$

(d) $(4, 7)$

Solution:

If $2+i\sqrt{3}$ is a root of the equation $x^2 + px + q = 0$, the other root will be $2-i\sqrt{3}$.

Sum of roots = $-p$

$$= 2+i\sqrt{3} + 2-i\sqrt{3}$$

$$= 4$$

$$\Rightarrow p = -4$$

Product of roots = q

$$= (2+i\sqrt{3})(2-i\sqrt{3})$$

$$= 4 + 2\sqrt{3}i - 2\sqrt{3}i + 3$$

$$= 7$$

So $(p, q) = (-4, 7)$

Hence option a is the answer.