Q12: The moment of inertia of a uniform cylinder of length and radius R about its perpendicular bisector is I. What is the ratio /R such that the moment of inertia is minimum?

- (a) 1
- (b)
- $3\sqrt{2}$
- (c)
- $\sqrt{3}/2$
- (d)
- $\sqrt{3/2}$

## Solution

Moment of Inertia I =  $m [I^2/12 + R^2/4]$ 

Volume =  $\pi R^2 I$ 

Writing Moment of inertia in terms of volume, we get

 $I = m/4(V/\pi l + I^2/3)$ 

Differentiating the above equation we get

 $dI/dI = m/4 (-V/\pi I^2 + 2I/3)$ 

For maxima and minima, dI/d/= 0

So m/4 (-V/ $\pi$ l<sup>2</sup> + 2I/3) = 0

 $V/\pi I^2 = 2I/3$ 

 $R^2/I = 2I/3 \text{ (Volume = } \pi R^2I\text{)}$ 

 $I^2/R^2 = 3/2$ 

$$l/R=\sqrt{rac{3}{2}}$$