

A 2 m ladder leans against a vertical wall. If the top of the ladder begins to slide down the wall at the rate 25 cm/sec., then the rate (in cm/sec.) at which the bottom of the ladder slides away from the wall on the horizontal ground when the top of the ladder is 1 m above the ground is:

[Main April 12, 2019 (I)]

(a)  $25\sqrt{3}$

(c)  $\frac{25}{3}$

(b)  $\frac{25}{\sqrt{3}}$

(d) 25

(b) According to the question,

$$\frac{dy}{dt} = -25 \text{ at } y = 1$$

By Pythagoras theorem,  $x^2 + y^2 = 4$  ... (i)

When  $y = 1 \Rightarrow x = \sqrt{3}$

Diff. equation (i) w. r. t.  $t$ ,

$$2x \frac{dx}{dt} + 2y \frac{dy}{dt} = 0$$

$$\Rightarrow x \frac{dx}{dt} + y \frac{dy}{dt} = 0$$

$$\Rightarrow \sqrt{3} \frac{dx}{dt} + (-25) = 0$$

$$\Rightarrow \frac{dx}{dt} = \frac{25}{\sqrt{3}} \text{ cm/s}$$