

7.31 In the LCR circuit the ac driving voltage is $v = v_m \sin \omega t$.

(i) Write down the equation of motion for $q(t)$.

(ii) At $t = t_0$, the voltage source stops and R is short-circuited. Now write down how much energy is stored in each of L and C.

(iii) Describe subsequent motion of charges.

Answer:

i) The equation for variation of motion of charge with respect to time is given as

$$L \frac{d^2q(t)}{dt^2} + R \frac{dq(t)}{dt} + q(t)/C = V_m \sin \omega t$$

ii) The energy stored in each of L and C is given as

$$U_c = \frac{1}{2} C \omega^2 [V_m^2 / R^2 + (XC - X_L)^2] \cos^2 (\omega t_0 + \phi)$$

iii) For the circuit to become LC oscillator, R needs to be short-circuited. By doing so, the capacitor will continue to discharge and all the energy will be transferred to L and back and forth. This way there will be an oscillation of energy from electrostatic to magnetic.