

A five-digit numbers divisible by 3 is to be formed using the numerals 0, 1, 2, 3, 4 and 5, without repetition. The total number of ways this can be done is (1989 - 2 Marks)

- (a) 216 (b) 240 (c) 600 (d) 3125

(d) We know that a number is divisible by 3 only when the sum of the digits is divisible by 3. The given digits are 0, 1, 2, 3, 4, 5.

Here the possible number of combinations of 5 digits out of 6 are ${}^5C_4 = 5$, which are as follows—

$$1 + 2 + 3 + 4 + 5 = 15 = 3 \times 5$$

$$0 + 2 + 3 + 4 + 5 = 14 \text{ (not divisible by 3)}$$

$$0 + 1 + 3 + 4 + 5 = 13 \text{ (not divisible by 3)}$$

$$0 + 1 + 2 + 4 + 5 = 12 = 3 \times 4$$

$$0 + 1 + 2 + 3 + 5 = 11 \text{ (not divisible by 3)}$$

$$0 + 1 + 2 + 3 + 4 = 10 \text{ (not divisible by 3)}$$

Thus the number should contain the digits 1, 2, 3, 4, 5 or the digits 0, 1, 2, 4, 5.

Taking 1, 2, 3, 4, 5, the 5 digit numbers are $= 5! = 120$

Taking 0, 1, 2, 4, 5, the 5 digit numbers are $= 5! - 4! = 96$

\therefore Total number of numbers $= 120 + 96 = 216$