

17 Find the differential equation of the family of lines through the origin.

Solution: Let $y = mx$ be the family of lines through origin.

$$\therefore \frac{dy}{dx} = m.$$

By eliminating m , we get $y = \frac{dy}{dx} \cdot x$ or $x \frac{dy}{dx} - y = 0.$