

Mean free path: -

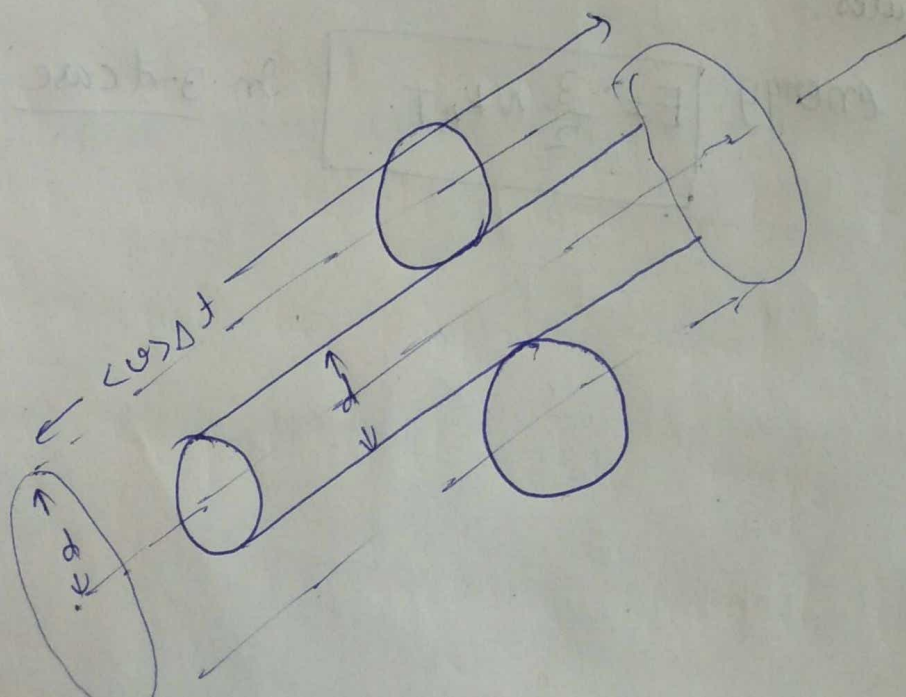
Molecules of in a gas have large speeds and they move and collide each other. As a result they can not move straight unhindered, their paths keep getting incessantly deflected.

Let us suppose, ~~we have~~ that we have n molecules of a gas of sphere of diameter d .

Let average speed of a single particle be $\langle v \rangle$.

then in time Δt ,

it covers $\pi d^2 \langle v \rangle \Delta t$ volume of cylinder.



If n is the no. of molecules per unit volume,

then no. of collisions in time $\Delta t = n\pi d^2 \langle v \rangle \Delta t$

So the rate of collisions is $n\pi d^2 \langle v \rangle$.

\therefore Time b/w two successive collisions

$$\tau = \frac{1}{n\pi \langle v \rangle d^2}$$

distance

mean free path :- The average distance b/w to successive collisions, called the mean free path.

$$\therefore d = \langle v \rangle \tau$$

$$d = \frac{1}{n\pi d^2}$$

but this is not correct. (here we assume rest of molecules in rest state)

$\rightarrow \therefore$ all molecules are moving,

\therefore exact mean free path (experiment)

mean free path

$$d = \frac{1}{\sqrt{2} \pi n d^2}$$

Vander Waals gas:-

As we know, there exists no ideal gas. All gases are real and follow Vander Waals equation.

For a real gas containing 'n' moles, the equation is written as,

$$\left(p + \frac{am^2}{v^2} \right) (v - nb) = nRT$$

where a & b are constant parameters and its values depend upon different gases.

→ Vander Waals assumed that, gaseous particles: —

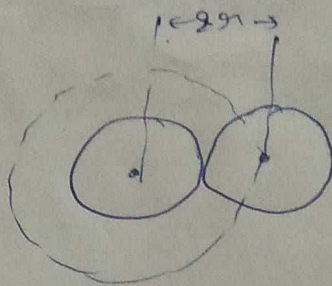
- i) Are hard spheres.
- ii) Have definite volume and hence can not be compressed beyond a limit
- iii) Two particles at close range interact and have an exclusive spherical volume around them.

Volume correction:-

$$V_R = V_i - b$$

Volume of real gas \downarrow
Volume of ideal gas \downarrow

correction factor \downarrow



$$b = 4 \times \frac{4}{3} \pi r^3 =$$

for particles, Volume correction = nb
 $= 4n \times \frac{4}{3} \pi r^3$

$$\therefore V_R = V_i - nb$$

Pressure correction:-

the reduction in pressure \propto square of particle density in the bulk \propto (due to surface particle)

$$\text{i.e. } \propto \frac{n^2}{V^2} = a \frac{n^2}{V^2}$$

$$\therefore \text{Pressure of real gas} = \frac{P}{V} + a \frac{n^2}{V^2}$$

Vander Waals gas equation:-

$$\left(P + a \frac{n^2}{V^2} \right) (V - nb) = nRT$$

for one particle
 $n=1$