

7. If potential energy between a proton and an electron is given by $|U| = ke^2/2R^3$, where e is the charge of electron and R is the radius of atom, then radius of Bohr's orbit is given by ($h =$ Planck's constant, $k =$ constant)

a. $\frac{ke^2 m}{h^2}$

b. $\frac{6\pi^2 ke^2 m}{n^2 h^2}$

c. $\frac{2\pi ke^2 m}{n h^2}$

d. $\frac{4\pi^2 ke^2 m}{n^2 h^2}$

$$\text{b. } U = -\frac{ke^2}{2R^3}, F = -\frac{dU}{dR} = -\frac{3ke^2}{2R^4}$$

$$\text{But, } F = \frac{mv^2}{R} \Rightarrow \frac{mv^2}{R} = \frac{3ke^2}{2R^4}$$

$$\text{Also, } mvR = \frac{nh}{2\pi}$$

$$\text{Solve to get: } R = \frac{6\pi^2 ke^2 m}{n^2 h^2}$$