

1. Newton's law of universal gravitation states that the gravitational force of attraction between any two particles of masses  $m_1$  and  $m_2$  separated by a distance  $r$  has the magnitude

$$F = G \frac{m_1 m_2}{r^2}$$

where  $G$  is the universal gravitational constant, which has the value  $6.672 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$ .

2. If we have to find the resultant gravitational force acting on the particle  $m$  due to a number of masses  $M_1, M_2, \dots, M_n$  etc. we use the principle of superposition. Let  $F_1, F_2, \dots, F_n$  be the individual forces due to  $M_1, M_2, \dots, M_n$ , each given by the law of gravitation. From the principle of superposition each force acts independently and uninfluenced by the other bodies. The resultant force  $F_R$  is then found by vector addition

$$F_R = F_1 + F_2 + \dots + F_n = \sum_{i=1}^n F_i$$

where the symbol ' $\Sigma$ ' stands for summation.

3. Kepler's laws of planetary motion state that

- (a) All planets move in elliptical orbits with the Sun at one of the focal points
- (b) The radius vector drawn from the Sun to a planet sweeps out equal areas in equal time intervals. This follows from the fact that the force of gravitation on the planet is central and hence angular momentum is conserved.
- (c) The square of the orbital period of a planet is proportional to the cube of the semi-major axis of the elliptical orbit of the planet

The period  $T$  and radius  $R$  of the circular orbit of a planet about the Sun are related by

$$T^2 = \left( \frac{4\pi^2}{G M_s} \right) R^3$$

where  $M_s$  is the mass of the Sun. Most planets have nearly circular orbits about the Sun. For elliptical orbits, the above equation is valid if  $R$  is replaced by the semi-major axis,  $a$ .

4. The acceleration due to gravity.

at a height  $h$  above the earth's surface

$$g(h) = \frac{G M_E}{(R_E + h)^2}$$
$$\approx \frac{G M_E}{R_E^2} \left( 1 - \frac{2h}{R_E} \right) \quad \text{for } h \ll R_E$$

$$g(h) = g(0) \left( 1 - \frac{2h}{R_E} \right) \quad \text{where } g(0) = \frac{G M_E}{R_E^2}$$