

Question

A particle of mass m is acted upon by a force F given by the empirical law $F = \frac{R}{t^2} v(t)$. If this law is to be tested experimentally by observing the motion starting from rest, the best way is to plot :

A $\log v(t)$ against $\frac{1}{t}$

B $v(t)$ against t^2

C $\log v(t)$ against $\frac{1}{t^2}$

D $\log v(t)$ against t

Solution

Correct option is A)

$$F = \frac{R}{t^2} v(t)$$

$$F = \frac{R}{t^2} v(t)$$

$$\Rightarrow m \frac{dv}{dt} = \frac{R}{t^2} v(t)$$

$$\Rightarrow \int \frac{dv}{v} = \int \frac{R dt}{m t^2}$$

$$\ln v = -\frac{R}{m t}$$

$$\Rightarrow \ln v \propto \frac{1}{t}$$