

Let  $\alpha$  and  $\beta$  be the roots of equation  $x^2 - 6x - 2 = 0$ . If  $a_n = \alpha^n - \beta^n$ , for  $n \geq 1$ , then the value of  $\frac{a_{10} - 2a_8}{2a_9}$  is equal to : [JEE-MAIN-2015]

(1) 3

(2) -3

(3) 6

(4) -6

Given  $x^2 - 6x - 2 = 0$

$\therefore a_{n+2} - 6a_{n+1} - 2a_n = 0$

$$\frac{a_{n+2} - 2a_n}{2a_{n+1}} = 3$$

Now, put  $n = 8$

$$\frac{a_{10} - 2a_8}{2a_9} = 3$$