If the roots of the equation $bx^2 + cx + a = 0$ be imaginary, then for all real values of x, the expression $3b^2x^2 + 6bcx + 2c^2$ is :- [AIEEE-2009]

(1) Greater than -4ab (2) Less than -4ab (3) Greater than 4ab (4) Less than 4ab

Since the roots of $bx^2 + cx + a = 0$ are imaginary

$$c^2 - 4ab < 0 \implies c^2 < 4ab$$

for exp. $3b^2x^2 + 6bcx + 2c^2$

Min. value =
$$\frac{-D}{4a} = \frac{(36b^2c^2 - 24b^2c^2)}{12b^2} = \frac{-12b^2c^2}{12b^2} = -c^2$$

$$\therefore$$
 - $c^2 > -4ab$

So exp. is greater than (- 4ab)