

Let two numbers have arithmetic mean 9 and geometric mean 4. Then these numbers are the roots of the quadratic equation

(a) $x^2 + 18x + 16 = 0$

(b) $x^2 - 18x - 16 = 0$

(c) $x^2 + 18x - 16 = 0$

(d) $x^2 - 18x + 16 = 0$

Solution:

Let m and n be the numbers.

$$(m + n)/2 = 9$$

$$(m + n) = 18$$

$$\sqrt{(mn)} = 4$$

$$mn = 16$$

So the equation is $x^2 - (\text{sum of roots})x + \text{product} = 0$

$$\Rightarrow x^2 - 18x + 16 = 0$$

Hence option d is the answer.