Circles - Class XI

Past Year JEE Questions

Questions

Quetion: 01

The circle $x^2 + y^2 = 4x + 8y + 5$ intersects the line 3x - 4y - m at two distinct points if

A.
$$-35 < m < 15$$

B.
$$15 < m < 65$$

C.
$$35 < m < 85$$

D.
$$-85 < m < -35$$

Solutions

Solution: 01

Explanation

Circle
$$x^2 + y^2 - 4x - 8y - 5 = 0$$

Center =
$$(2, 4)$$
, Radius = $\sqrt{4 + 16 + 5} = 5$

If circle is intersecting line 3x - 4y = m, at two distinct points.

 \Rightarrow length of perpendicular from center to the line < radius

$$\Rightarrow \frac{|6-16-m|}{5} \stackrel{\textstyle <}{<} 5 \Rightarrow |10+m| < 25$$

$$\Rightarrow -25 < m+10 < 25 \Rightarrow -35 < m < 15$$