

The sum of the series $\sum_{n=8}^{17} \frac{1}{(n+2)(n+3)}$ is equal to

1. $\frac{1}{17}$

2. $\frac{1}{18}$

3. $\frac{1}{19}$

4. $\frac{1}{20}$

Solution:

$$S = \sum_{n=8}^{17} \frac{1}{(n+2)(n+3)}$$

$$= \sum_{n=8}^{17} \left(\frac{1}{n+2} - \frac{1}{n+3} \right)$$

$$= \left(\frac{1}{10} - \frac{1}{11} \right) + \left(\frac{1}{11} - \frac{1}{12} \right) + \dots + \left(\frac{1}{19} - \frac{1}{20} \right)$$

$$= \frac{1}{10} - \frac{1}{20}$$

$$= \frac{1}{20}$$

Hence option (4) is the answer.