

### Question

A prism of refractive index  $\mu$  and angle  $A$  is placed in the minimum deviation position. If the angle of minimum deviation is  $A$ , then the value of  $A$  in terms of  $\mu$  is:

A  $\sin^{-1}\left(\frac{\mu}{2}\right)$

B  $\sin^{-1}\sqrt{\frac{\mu-1}{2}}$

C  $2\cos^{-1}\left(\frac{\mu}{2}\right)$

D  $2\cos^{-1}\left(\frac{\mu}{8}\right)$

### Solution

Correct option is C)

We can use the formula:  $\mu = \frac{\sin\left(\frac{A+D}{2}\right)}{\sin\left(\frac{A}{2}\right)}$

where  $D$  is angle of minimum deviation and  $A$  is angle of prism.

According to given condition  $A = D$

$$\therefore \mu = \frac{\sin\left(\frac{A+A}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$$\mu = \frac{\sin(A)}{\sin\left(\frac{A}{2}\right)}$$

$$\mu = \frac{2\sin\left(\frac{A}{2}\right)\cos\left(\frac{A}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$$\mu = 2\cos\left(\frac{A}{2}\right)$$

$\therefore A = 2\cos^{-1}\left(\frac{\mu}{2}\right)$  which is the required solution.