Question 10: It S is the set of distinct values of 'b' for which the following system of linear equations x + y + z = 1x + ay + z = 1 ax + by + z = 0 has no solution, then S is:

- (a) an empty set
- (b) an infinite set
- (c) a finite set containing two or more elements
- (d) a singleton

Answer: (d)

Solution:

$$D = \begin{vmatrix} 1 & 1 & 1 \\ 1 & a & 1 \\ a & b & 1 \end{vmatrix}$$

$$= -(a-1)^2 = 0$$

We get first two planes co-incident for a = 1.

$$x + y + z = 1$$

$$x + y + z = 1$$

$$x + by + z = 0$$

If b = 1, the system will be inconsistent and hence no solution.

If $b \neq 1$, the system will produce infinite solutions.

Hence, for no solution, S has to be a singleton set {1}.