JEE Main 2020 (Online) 2nd September Evening Slot

If the variance of the terms in an increasing A.P.,

 b_1 , b_2 , b_3 ,..., b_{11} is 90, then the common difference of this A.P. is_____.

Answer

Correct Answer is 3

Explanation

Let the common difference = d

and
$$b_1=a$$

$$b_2 = a + d$$

$$b_3 = a + 2d$$

$$...b_{11} = a + 10d$$

Variance =
$$rac{\sum a_i^2}{11} - \left(rac{\sum a_i}{11}
ight)^2 = 90$$

$$\Rightarrow \frac{a^2 + (a+d)^2 + ... + (a+10d)^2}{11} - \left(\frac{a + (a+d) + ... + (a+10d)}{11}\right)^2 = 90$$

$$\Rightarrow 11 \left[11a^2 + 385d^2 + 110ad \right] - \left[11a + 55d \right]^2 = 10890$$

$$\Rightarrow 1210d^2 = 10890$$

$$\Rightarrow d^2 = 9$$

$$\Rightarrow d = \pm 3$$

As A.P is increasing so d should be positive