

Q. Let  $I$  be the purchase value of an equipment and  $V(t)$  be the value after it has been used for  $t$  years. The value  $V(t)$  depreciates at a rate given by differential equation  $\frac{dV(t)}{dt} = -k(T - t)$  where  $k > 0$  is a constant and  $T$  is the total life in years of the equipment. Then the scrap value  $V(T)$  of the equipment is :- (1)  $I - \frac{k(T-t)^2}{2}$  (2)  $e^{-kT}$  (3)  $T^2 - \frac{I}{k}$  (4)  $I - \frac{kT^2}{2}$  [AIEEE-2011]

**1 JEE Main 2021 (Online) 27th August Evening Shift**

MCQ (Single Correct Answer)

If the solution curve of the differential equation  $(2x - 10y^3)dy + ydx = 0$ , passes through the points  $(0, 1)$  and  $(2, \beta)$ , then  $\beta$  is a root of the equation :

**A**  $y^5 - 2y - 2 = 0$

**B**  $2y^5 - 2y - 1 = 0$

**C**  $2y^5 - y^2 - 2 = 0$

**D**  $y^5 - y^2 - 1 = 0$

### Explanation

$$(2x - 10y^3)dy + ydx = 0$$

$$\Rightarrow \frac{dx}{dy} + \left(\frac{2}{y}\right)x = 10y^2$$

$$I.F. = e^{\int \frac{2}{y} dy} = e^{2\ln(y)} = y^2$$

Solution of D.E. is

$$\therefore x \cdot y = \int (10y^2)y^2 \cdot dy$$

$$xy^2 = \frac{10y^5}{5} + C \Rightarrow xy^2 = 2y^5 + C$$

It passes through  $(0, 1) \rightarrow 0 = 2 + C \Rightarrow C = -2$

Now, it passes through  $(2, \beta)$

$$2\beta^2 = 2\beta^5 - 2 \Rightarrow \beta^5 - \beta^2 - 1 = 0$$

$$\therefore \beta \text{ is root of an equation } y^5 - y^2 - 1 = 0$$