

The sum of the distinct real values of μ , for which the vectors, $\mu\hat{i} + \hat{j} + \hat{k}$, $\hat{i} + \mu\hat{j} + \hat{k}$, $\hat{i} + \hat{j} + \mu\hat{k}$, are co-planar,

is :

(1) -1

(2) 0

(3) 1

(4) 2

Ans

$$\mu \hat{i} + \hat{j} + \hat{k}, \quad \hat{i} + \mu \hat{j} + \hat{k}, \quad \hat{i} + \hat{j} + \mu \hat{k}$$

$$\begin{vmatrix} \mu & 1 & 0 \\ 1 & \mu & 1 \\ 1 & 1 & \mu \end{vmatrix} = 0$$

$$\mu(\mu^2 - 1) - 1(\mu - 1) + 1(1 - \mu) = 0$$

$$\mu^3 - \mu - \mu + 1 + 1 - \mu = 0$$

$$\mu^3 - 3\mu + 2 = 0$$

$$\text{Sum} = 0$$