Q. No. 4: Find a vector in the direction of a vector $5\hat{i}-\hat{j}+2\hat{k}$ which has a magnitude of 8 units.

Solution:

Let
$$ec{a}=5\hat{i}-\hat{j}+2\hat{k}$$

$$|\vec{a}| = \sqrt{5^2 + (-1)^2 + 2^2} = \sqrt{25 + 1 + 4} = \sqrt{30}$$
$$\therefore \hat{a} = \frac{\vec{a}}{|\vec{a}|} = \frac{5\hat{i} - \hat{j} + 2\hat{k}}{\sqrt{30}}$$

Hence, the vector in the direction of vector $\hat{5i}-\hat{j}+2\hat{k}$ which has a magnitude of 8 units is given by

$$8\hat{a} = 8\left(\frac{5\hat{i} - \hat{j} + 2\hat{k}}{\sqrt{30}}\right)$$
$$= \frac{40}{\sqrt{30}}\hat{i} - \frac{8}{\sqrt{30}}\hat{j} + \frac{16}{\sqrt{30}}\hat{k}$$