

Question 1: If a , b and c are unit vectors, then $|a - b|^2 + |b - c|^2 + |c - a|^2$ does not exceed

A) 4

B) 9

C) 8

D) 6

Ans $|a-b|^2 + |b-c|^2 + |c-a|^2$

$$= 2(a^2 + b^2 + c^2) - 2(ab + bc + ca)$$

and $|a| = |b| = |c| = 1$

$$= 6 - \left[(a+b+c)^2 - a^2 - b^2 - c^2 \right]$$

$$= 6 - (a+b+c)^2 + 3$$

$$= 9 - (a+b+c)^2 \leq 9$$

Ans B