

- 2.** The sum of all natural numbers ' n ' such that $100 < n < 200$ and $\text{HCF}(91, n) > 1$ is

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- (a) 3203 (b) 3303
(c) 3221 (d) 3121

Exp. (d)

The natural numbers between 100 and 200 are 101, 102, 103, ..., 199.

Since, $91 = 13 \times 7$, so the natural numbers between 100 and 200 whose HCF with 91 is more than 1 are the numbers which are either divisible by 7 or 13.

So, the required sum of numbers between 100 and 200 = (sum of numbers divisible by 7) + (sum of numbers divisible by 13) - (sum of numbers divisible by 91)

$$\begin{aligned} &= \sum_{r=1}^{14} (98 + 7r) + \sum_{r=1}^8 (91 + 13r) - (182) \\ &= (98 \times 14) + 7 \left(\frac{14 \times 15}{2} \right) + (91 \times 8) \\ &\quad + 13 \left(\frac{8 \times 9}{2} \right) - (182) \\ &= 1372 + 735 + 728 + 468 - 182 \\ &= 3303 - 182 \\ &= 3121 \end{aligned}$$