

Special Series

Special Series is a series which is special in some way. It could be arithmetic or geometric.

Some of the special series are:

1. Sum of first n natural numbers: $1 + 2 + 3 + 4 + \dots + n$
2. Sum of squares of first n natural numbers: $1^2 + 2^2 + 3^2 + 4^2 + \dots + n^2$
3. Sum of cubes of first n natural numbers: $1^3 + 2^3 + 3^3 + 4^3 + \dots + n^3$

Some standard results:

1. Sum of first n natural numbers

$$\sum_{r=1}^n r = \frac{n(n+1)}{2}$$

2. Sum of first n odd natural numbers

$$\sum_{r=1}^n (2r-1) = n^2$$

3. Sum of first n even natural numbers

$$\sum_{r=1}^n 2r = n(n+1)$$