

**NCERT Exemplar MCQs**

- Let  $T$  be the set of all triangles in the Euclidean plane and let a relation  $R$  on  $T$  be defined as  $aRb$ , if  $a$  is congruent to  $b$ ,  $\forall a, b \in T$ . Then,  $R$  is
  - reflexive but not transitive
  - transitive but not symmetric
  - equivalence
  - None of these
- Consider the non-empty set consisting of children in a family and a relation  $R$  defined as  $aRb$  if  $a$  is brother of  $b$ . Then  $R$  is
  - symmetric but not transitive
  - transitive but not symmetric
  - neither symmetric nor transitive
  - both symmetric and transitive
- The maximum number of equivalence relations on the set  $A = \{1, 2, 3\}$  are
  - 1
  - 2
  - 3
  - 5
- If a relation  $R$  on set  $\{1, 2, 3\}$  be defined by  $R = \{(1, 2)\}$ , then  $R$  is
  - reflexive
  - transitive
  - symmetric
  - None of these
- Let us define a relation  $R$  in  $\mathbb{R}$  as  $aRb$  if  $a \geq b$ . Then  $R$  is
  - an equivalence relation
  - reflexive, transitive but not symmetric
  - symmetric, transitive but not reflexive
  - neither transitive nor reflexive but symmetric
- The relation  $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3), (1, 3)\}$  on set  $A = \{1, 2, 3\}$  is
  - Reflexive but not symmetric
  - Reflexive but not transitive
  - Symmetric and transitive
  - Neither symmetric nor transitive
- The identity element for the binary operation  $*$  defined on  $Q - \{0\}$  as  $a * b = \frac{ab}{2}$ ,  $\forall a, b \in Q - \{0\}$  is
  - 1
  - 0
  - 2
  - None of these
- If the set  $A$  contains 5 elements and the set  $B$  contains 6 elements, then the number of one-one and onto mapping from  $A$  to  $B$  is
  - 720
  - 120
  - 0
  - None of these
- If  $A = \{1, 2, 3, \dots, n\}$  and  $B = \{a, b\}$ . Then, the number of surjections from  $A$  into  $B$  is
  - ${}^n P_2$
  - $2^n - 2$
  - $2^n - 1$
  - None of these

- Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = \frac{1}{x} \forall x \in \mathbb{R}$ . Then  $f$  is
  - one-one
  - onto
  - bijective
  - $f$  is not defined
- Let  $f: \mathbb{R} \rightarrow \mathbb{R}$  be defined by  $f(x) = 3x^2 - 5$  and  $g: \mathbb{R} \rightarrow \mathbb{R}$  by  $g(x) = \frac{x}{x^2 + 1}$ . Then  $g \circ f$  is
  - $\frac{3x^2 - 5}{9x^4 - 30x^2 + 26}$
  - $\frac{3x^2 - 5}{9x^4 - 6x^2 + 26}$
  - $\frac{3x^2}{x^4 + 2x^2 - 4}$
  - $\frac{3x^2}{9x^4 + 30x^2 - 2}$
- Which of the following functions from  $Z$  into  $Z$  are bijective?
  - $f(x) = x^3$
  - $f(x) = x + 2$
  - $f(x) = 2x + 1$
  - $f(x) = x^2 + 1$
- If  $f: \mathbb{R} \rightarrow \mathbb{R}$  be the function defined by  $f(x) = x^3 + 5$ , then  $f^{-1}(x)$  is equal to:
  - $(x + 5)^{1/3}$
  - $(x - 5)^{1/3}$
  - $(5 - x)^{1/3}$
  - $(5 - x)$
- If  $f: A \rightarrow B$  and  $g: B \rightarrow C$  be the bijective functions, then  $(g \circ f)^{-1}$  is
  - $f^{-1} \circ g^{-1}$
  - $f \circ g$
  - $g^{-1} \circ f^{-1}$
  - $g \circ f$
- Let  $f: \mathbb{R} - \left\{\frac{3}{5}\right\} \rightarrow \mathbb{R}$  be defined by  $f(x) = \frac{3x + 2}{5x - 3}$ . Then
  - $f^{-1}(x) = f(x)$
  - $f^{-1}(x) = -f(x)$
  - $(f \circ f)x = -x$
  - $f^{-1}(x) = \frac{1}{19}f(x)$
- If  $f(x)$  is defined on  $[0, 1]$  by the rule
 
$$f(x) = \begin{cases} x & : x \text{ is rational} \\ 1 - x & : x \text{ is irrational} \end{cases}$$
 then for all  $x \in \mathbb{R}$ ,  $f(f(x))$  is
  - constant
  - $1 + x$
  - $x$
  - None of these
- If  $f: [2, \infty) \rightarrow \mathbb{R}$  be the function defined by  $f(x) = x^2 - 4x + 5$ , then the range of  $f$  is
  - $\mathbb{R}$
  - $[1, \infty)$
  - $[4, \infty)$
  - $[5, \infty)$
- Let  $f: \mathbb{N} \rightarrow \mathbb{R}$  be the function defined by
  - ${}^n P_2$
  - $2^n - 2$
  - $2^n - 1$
  - None of these

$f(x) = \frac{2x-1}{2}$  and  $g: Q \rightarrow R$  be another function defined by  $g(x) = x + 2$ . Then  $(g \circ f) \frac{3}{2}$  is

- (a) 1      (b) 0      (c)  $\frac{7}{2}$       (d) 3

19. Let  $f: R \rightarrow R$  be defined by

$$f(x) = \begin{cases} 2x & : x > 3 \\ x^2 & : 1 < x \leq 3 \\ 3x & : x \leq 1 \end{cases}$$

Then  $f(-1) + f(2) + f(4)$  is

- (a) 9      (b) 14  
(c) 5      (d) None of these

20. Let  $f: R \rightarrow R$  be given by  $f(x) = \tan x$ . Then  $f^{-1}(1)$  is

- (a)  $\frac{\pi}{4}$       (b)  $\left\{ n\pi + \frac{\pi}{4} : n \in Z \right\}$   
(c) does not exist      (d) None of these

#### Past Year MCQs

21. If  $g$  is the inverse of a function  $f$  and  $f'(x) = \frac{1}{1+x^5}$ , then

$g'(x)$  is equal to: [JEE MAIN 2014, C]

- (a)  $\frac{1}{1+\{g(x)\}^5}$       (b)  $1+\{g(x)\}^5$   
(c)  $1+x^5$       (d)  $5x^4$

22. Let  $f: R \rightarrow R$  be a function defined by  $f(x) = \frac{x-m}{x-n}$ ,

where  $m \neq n$ , then [BITSAT 2014, A]

- (a)  $f$  is one-one onto      (b)  $f$  is one-one into  
(c)  $f$  is many-one onto      (d)  $f$  is many-one into

23. If  $\rho = \{(x, y) | x^2 + y^2 = 1; x, y \in R\}$ . Then,  $\rho$  is [BITSAT 2015, A]

- (a) reflexive      (b) symmetric  
(c) transitive      (d) anti-symmetric

24. Let  $f(x) = \frac{ax+b}{cx+d}$ , then  $f \circ f(x) = x$ , provided that :

[BITSAT, 2016, A]

- (a)  $d = -a$       (b)  $d = a$   
(c)  $a = b = 1$       (d)  $a = b = c = d = 1$

25. The function  $f: R \rightarrow \left[-\frac{1}{2}, \frac{1}{2}\right]$  defined as  $f(x) = \frac{x}{1+x^2}$ , is :

[JEE MAIN 2017, A]

- (a) neither injective nor surjective  
(b) invertible  
(c) injective but not surjective  
(d) surjective but not injective

26. Let  $f$  and  $g$  be functions from  $R$  to  $R$  defined as

$$f(x) = \begin{cases} 7x^2 + x - 8, & x \leq 1 \\ 4x + 5, & 1 < x \leq 7 \\ 8x + 3, & x > 7 \end{cases}, \quad g(x) = \begin{cases} |x|, & x < -3 \\ 0, & -3 \leq x < 2 \\ x^2 + 4, & x \geq 2 \end{cases}$$

Then [BITSAT 2017, S]

- (a)  $(f \circ g)(-3) = 8$       (b)  $(f \circ g)(9) = 683$   
(c)  $(g \circ f)(0) = -8$       (d)  $(g \circ f)(6) = 427$

**Ans.**

<b>1</b>	(c)	<b>4</b>	(d)	<b>7</b>	(c)	<b>10</b>	(d)	<b>13</b>	(b)	<b>16</b>	(c)	<b>19</b>	(a)	<b>22</b>	(b)	<b>25</b>	(d)		
<b>2</b>	(b)	<b>5</b>	(b)	<b>8</b>	(c)	<b>11</b>	(a)	<b>14</b>	(a)	<b>17</b>	(b)	<b>20</b>	(b)	<b>23</b>	(b)	<b>26</b>	(b)		
<b>3</b>	(d)	<b>6</b>	(a)	<b>9</b>	(d)	<b>12</b>	(b)	<b>15</b>	(a)	<b>18</b>	(d)	<b>21</b>	(b)	<b>24</b>	(a)				