

### Topic 1 : Types of Relations.

- Let  $P = \{(x, y) \mid x^2 + y^2 = 1, x, y \in \mathbb{R}\}$ . Then,  $P$  is
  - Reflexive
  - Symmetric
  - Transitive
  - Anti-symmetric
- For real numbers  $x$  and  $y$ , we write  $x R y \Leftrightarrow x - y + \sqrt{2}$  is an irrational number. Then, the relation  $R$  is
  - Reflexive
  - Symmetric
  - Transitive
  - None of these
- Let  $L$  denote the set of all straight lines in a plane. Let a relation  $R$  be defined by  $\alpha R \beta \Leftrightarrow \alpha \perp \beta, \alpha, \beta \in L$ . Then,  $R$  is
  - Reflexive
  - Symmetric
  - Transitive
  - None of these
- Let  $S$  be the set of all real numbers. Then, the relation  $R = \{(a, b) : 1 + ab > 0\}$  on  $S$  is
  - Reflexive and symmetric but not transitive
  - Reflexive and transitive but not symmetric
  - Symmetric, transitive but not reflexive
  - Reflexive, transitive and symmetric
- Let  $R$  be a relation on the set  $N$  be defined by  $\{(x, y) \mid x, y \in N, 2x + y = 41\}$ . Then,  $R$  is
  - Reflexive
  - Symmetric
  - Transitive
  - None of these
- Let  $A = \{1, 2, 3\}$  and  $B = \{2, 4, 6, 8\}$ . Consider the rule  $f : A \rightarrow B, f(x) = 2x \forall x \in A$ . The domain, codomain and range of  $f$  respectively are
  - $\{1, 2, 3\}, \{2, 4, 6\}, \{2, 4, 6, 8\}$
  - $\{1, 2, 3\}, \{2, 4, 6, 8\}, \{2, 4, 6\}$
  - $\{2, 4, 6, 8\}, \{2, 4, 6, 7\}, \{1, 2, 3\}$
  - $\{2, 4, 6\}, \{2, 4, 6, 8\}, \{1, 2, 3\}$
- The relation "less than" in the set of natural numbers is :
  - only symmetric
  - only transitive
  - only reflexive
  - equivalence relation
- Let  $R$  and  $S$  be two non-void relations in a set  $A$ . Which of the following statements is not true.
  - $R$  and  $S$  transitive  $\Rightarrow R \cup S$  is transitive
  - $R$  and  $S$  transitive  $\Rightarrow R \cap S$  is transitive
  - $R$  and  $S$  symmetric  $\Rightarrow R \cup S$  is symmetric
  - $R$  and  $S$  reflexive  $\Rightarrow R \cap S$  is reflexive
- The relation  $R = \{(1, 1), (2, 2), (3, 3)\}$  on the set  $\{1, 2, 3\}$  is :
  - symmetric only
  - reflexive only
  - an equivalence relation
  - transitive only
- Let  $A$  be the non-empty set of children in a family. The relation 'x is brother of y' in  $A$  is:
  - reflexive
  - symmetric
  - transitive
  - None of these
- Let  $A = \{1, 2, 3, 4\}$  and let  $R = \{(2, 2), (3, 3), (4, 4), (1, 2)\}$  be a relation on  $A$ . Then  $R$  is:
  - reflexive
  - symmetric
  - transitive
  - None of these
- If  $R$  is a relation in a set  $A$  such that  $(a, a) \in R$  for every  $a \in A$ , then the relation  $R$  is called
  - symmetric
  - reflexive
  - transitive
  - symmetric or transitive
- A relation  $R$  in a set  $A$  is called empty relation, if
  - no element of  $A$  is related to any element of  $A$
  - every element of  $A$  is related to every element of  $A$
  - some elements of  $A$  are related to some elements of  $A$
  - None of the above
- A relation  $R$  in a set  $A$  is called universal relation, if
  - each element of  $A$  is not related to every element of  $A$
  - no element of  $A$  is related to any element of  $A$
  - each element of  $A$  is related to every element of  $A$
  - None of the above
- A relation  $R$  in a set  $A$  is said to be an equivalence relation, if  $R$  is
  - symmetric only
  - reflexive only
  - transitive only
  - All of these
- Let  $R = \{(3, 3), (5, 5), (9, 9), (12, 12), (5, 12), (3, 9), (3, 12), (3, 5)\}$  be a relation on the set  $A = \{3, 5, 9, 12\}$ . Then,  $R$  is:
  - reflexive, symmetric but not transitive.
  - symmetric, transitive but not reflexive.
  - an equivalence relation.
  - reflexive, transitive but not symmetric.
- A relation  $R$  in a set  $A$  is called transitive, if for all  $a_1, a_2, a_3 \in A, (a_1, a_2) \in R$  and  $(a_2, a_3) \in R$  implies
  - $(a_2, a_1) \in R$
  - $(a_1, a_3) \in R$
  - $(a_3, a_1) \in R$
  - $(a_3, a_2) \in R$
- If  $R = \{(x, y) : x \text{ is father of } y\}$ , then  $R$  is
  - reflexive but not symmetric
  - symmetric and transitive
  - neither reflexive nor symmetric nor transitive
  - Symmetric but not reflexive
- If  $R = \{(x, y) : x \text{ is exactly 7 cm taller than } y\}$ , then  $R$  is
  - not symmetric
  - reflexive
  - symmetric but not transitive
  - an equivalence relation
- If  $R = \{(x, y) : x \text{ is wife of } y\}$ , then  $R$  is
  - reflexive
  - symmetric
  - transitive
  - an equivalence relation
- Let  $R$  be the relation in the set  $Z$  of all integers defined by  $R = \{(x, y) : x - y \text{ is an integer}\}$ . Then  $R$  is
  - reflexive
  - symmetric
  - transitive
  - an equivalence relation
- Let  $R$  be the relation in the set  $\{1, 2, 3, 4\}$  given by  $R = \{(1, 2), (2, 2), (1, 1), (4, 4), (1, 3), (3, 3), (3, 2)\}$ .
  - $R$  is reflexive and symmetric but not transitive
  - $R$  is reflexive and transitive but not symmetric
  - $R$  is symmetric and transitive but not reflexive
  - $R$  is equivalence relation

# Ans.

1	(b)
2	(a)
3	(b)
4	(a)
5	(d)
6	(b)
7	(b)
8	(a)
9	(b)
10	(c)
11	(c)
12	(b)
13	(a)
14	(c)

15	(d)
16	(d)
17	(b)
18	(c)
19	(a)
20	(c)
21	(d)
22	(b)