

Question 5: If $f(x) = \frac{x-3}{x+1}$

, then $f[f\{f(x)\}]$ equals _____.

Solution:

$$f[f(x)] = f(x) - 3f(x) + 1$$

$$= \frac{x-3}{x+1} - 3\frac{x-3}{x+1} + 1$$

$$= \frac{x-3-3x+9}{2x-2}$$

$$= \frac{x+3}{1-x}$$

$$f(x) = (2, 4] - \{3\}.$$

$$\text{Now } f[f\{f(x)\}] = f\left(\frac{3+x}{1-x}\right)$$