

If A and B are two events such that $P(B) = \frac{3}{5}$, $P(A/B) = \frac{1}{2}$ and $P(A \cup B) = \frac{4}{5}$, then $P(A)$ equals to

(a) $\frac{3}{10}$

(b) $\frac{1}{5}$

(c) $\frac{1}{2}$

(d) $\frac{3}{5}$

Here, $P(B) = \frac{3}{5}$, $P(A/B) = \frac{1}{2}$ and $P(A \cup B) = \frac{4}{5}$

$$\therefore P(A/B) = \frac{P(A \cap B)}{P(B)}$$

$$\Rightarrow \frac{1}{2} = \frac{P(A \cap B)}{3/5}$$

$$\Rightarrow P(A \cap B) = \frac{3}{5} \times \frac{1}{2} = \frac{3}{10}$$

and $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

$$\Rightarrow \frac{4}{5} = P(A) + \frac{3}{5} - \frac{3}{10}$$

$$\therefore P(A) = \frac{4}{5} - \frac{3}{5} + \frac{3}{10} = \frac{8 - 6 + 3}{10} = \frac{1}{2}$$