

1. Let  $R$  be the relation on the set  $\mathbb{R}$  of all real numbers defined by  $a R b$  if and only if  $|a - b| \leq 1$ . Then  $R$  is \_\_\_\_\_.

Solution:  $|a - a| = 0 < 1$

Therefore,  $a R a \forall a \in \mathbb{R}$

Therefore,  $R$  is reflexive.

Again  $a R b, |a - b| \leq 1 \Rightarrow |b - a| \leq 1 \Rightarrow b R a$

Therefore,  $R$  is symmetric.

Again  $1 R [\frac{1}{2}]$  and  $[\frac{1}{2}] R 1$  but  $[\frac{1}{2}] \neq 1$

Therefore,  $R$  is not anti-symmetric.

Further,  $1 R 2$  and  $2 R 3$  but  $1 \not R 3$ , [Because,  $|1 - 3| = 2 > 1$ ]

Hence,  $R$  is not transitive.