

Circles - Class XI

Past Year JEE Questions

Questions

Question: 01

The number of integral values of k for which the line, $3x + 4y = k$ intersects the circle, $x^2 + y^2 - 2x - 4y + 4 = 0$ at two distinct points is _____.

Solutions

Solution: 01

Answer

Correct Answer is **9**

Explanation

Circle $x^2 + y^2 - 2x - 4y + 4 = 0$

$$\Rightarrow (x - 1)^2 + (y - 2)^2 = 1$$

Centre: (1, 2), radius = 1

Line $3x + 4y - k = 0$ intersects the circle at two distinct points.

\Rightarrow distance of centre from the line $<$ radius

$$\Rightarrow \left| \frac{3 \times 1 + 4 \times 2 - k}{\sqrt{3^2 + 4^2}} \right| < 1$$

$$\Rightarrow |11 - k| < 5$$

$$\Rightarrow 6 < k < 16$$

$\Rightarrow k \in \{7, 8, 9, \dots, 15\}$ since $k \in \mathbb{I}$

\therefore Total 9 integral value of k .