

Matrices - Class XII

Past Year JEE Questions

Questions

Question: 01

If the following system of linear equations

$$2x + y + z = 5$$

$$x - y + z = 3$$

$$x + y + az = b$$

has no solution, then :

A. $a = -\frac{1}{3}, b \neq \frac{7}{3}$

B. $a \neq \frac{1}{3}, b = \frac{7}{3}$

C. $a \neq -\frac{1}{3}, b = \frac{7}{3}$

D. $a = \frac{1}{3}, b \neq \frac{7}{3}$

Solutions

Solution: 01

Explanation

$$\text{Here } D = \begin{vmatrix} 2 & 1 & 1 \\ 1 & -1 & 1 \\ 1 & 1 & a \end{vmatrix} = 2(a-1) - 1(a-1) + 1 + 1 \\ = 1 - 3a$$

$$D_3 = \begin{vmatrix} 2 & 1 & 5 \\ 1 & -1 & 3 \\ 1 & 1 & b \end{vmatrix} = 2(-b-3) - 1(b-3) + 5(1+1) \\ = 7 - 3b$$

for $a = \frac{1}{3}, b \neq \frac{7}{3}$, system has no solutions.