

(5) Let A be a set of all 4-digit numbers (natural) whose exactly one digit is 7. Then the probability that a randomly chosen element of A leaves remainder 2 when divided by 5 is:

Soln: Total no. of cases =

$$\begin{aligned} & n(\text{when } 7 \text{ appears on } 1000\text{'s place}) \\ & + n(\text{when } 7 \text{ does not appear on } 1000\text{'s place}) \\ & = (9 \times 9 \times 9) + (8 \times 9 \times 9 \times 3) \\ & = 9 \times 9 \times 33 \end{aligned}$$

Favourable cases =

$$\begin{aligned} & n(\text{last digit } 7 \text{ \& } 7 \text{ appear once}) \\ & + n(\text{last digit } 2 \text{ \& } 7 \text{ appear once}) \\ & = (8 \times 9 \times 9) + [(9 \times 9) + (8 \times 9 \times 2)] \\ & = 8 \times 9 \times 9 + 25 \times 9. \end{aligned}$$

$$\therefore P(E) = \frac{8 \times 9 \times 9 + 25 \times 9}{9 \times 9 \times 33} = \frac{97}{297}$$