

A signal of 0.1 kW is transmitted in a cable. The attenuation of cable is -5 dB per km and cable length is 20 km. The power received at receiver is 10^{-x} W. The value of x is _____.

$$[\text{Gain in } dB = 10 \log_{10} \left(\frac{P_o}{P_i} \right)]$$

Given, power of transmitted signal, $P_i = 0.1 \text{ kW} = 0.1 \times 10^3 \text{ W} = 10^2 \text{ W}$

Rate of attenuation, $R = -5 \text{ dB/km}$

Length of cable, $l = 20 \text{ km}$

Power received at receiver, $P_x = 10^{-x} \text{ W}$

Total loss, $\beta = R \times l = -5 \times 20 = -100 \text{ dB}$

$$\therefore \text{Gain } (\beta) = 10 \log_{10} \frac{P_0}{P_i}$$

$$\therefore \beta = -100 = -10 \log_{10} \frac{P_0}{P_i}$$

$$\Rightarrow -10 = \log_{10} \frac{P_0}{P_i} \Rightarrow 10^{-10} = \frac{P_0}{P_i}$$

$$\Rightarrow P_0 = 10^{-10} P_i = 10^{-10} \times 10^2 = 10^{-8} \Rightarrow P_0 = 10^{-8} \text{ W}$$

Hence, $x = 8$