

Matrices - Class XII

Related Questions with Solutions

Questions

Question: 01

If the system of linear equations :

$$x + ay + z = 3$$

$$x + 2y + 2z = 6$$

$$x + 5y + 3z = b$$

has no solution, then

A. $a = -1, b = 9$

B. $a \neq -1, b = 9$

C. $a = 1, b \neq 9$

D. $a = -1, b \neq 9$

Question: 02

The number of values of k , for which the system of equations $(k + 1)x + 8y = 4k, kx + (k + 3)y = 3k - 1$ has no solution, is

A. 1

B. 2

C. 3

D. infinite

Question: 03

Consider the system of linear equations

$$x_1 + 2x_2 + x_3 = 3$$

$$2x_1 + 3x_2 + x_3 = 3$$

$$3x_1 + 5x_2 + 2x_3 = 1$$

The system has

A. infinite number of solutions

B. exactly 3 solutions

C. a unique solution

D. no solution

Question: 04

The system of equations

$\alpha x + y + z = \alpha - 1, x + \alpha y + z = \alpha - 1, x + y + \alpha z = \alpha - 1$ has no solutions, if α is

A. either -2 or 1

B. -2

C. 1

D. not -2

Question: 05

The values of k for which the system $(k + 1)x + 8y = 0; kx + (k + 3)y = 0$ has unique solution, are

A. 3, 1

B. -3, 1

C. 3, -1

D. -3, -1

Question: 06

The number of real values of λ for which the system of linear equations $2x + 4y - \lambda z = 0, 4x + \lambda y + 2z = 0, \lambda x + 2y + 2z = 0$ has infinitely many solutions, is

A. 0

- B. 1
C. 2
D. 3

Solutions

Solution: 01

The given system of equations has no solution.

$$\therefore \begin{vmatrix} 1 & a & 1 \\ 1 & 2 & 2 \\ 1 & 5 & 3 \end{vmatrix} = 0$$

Applying $R_1 \rightarrow R_1 - R_2$ and then $R_2 \rightarrow R_2 - R_3$, we get

$$\begin{vmatrix} 0 & a-2 & -1 \\ 0 & -3 & -1 \\ 1 & 5 & 3 \end{vmatrix} = 0 \Rightarrow a = -1$$

Also in addition to above $(\text{adj } A)B \neq O \Rightarrow$ no solution

$$\text{Here, } \text{adj}(A) = \begin{bmatrix} -4 & 8 & -4 \\ -1 & 2 & -1 \\ 3 & -6 & 3 \end{bmatrix}$$

$$\Rightarrow (\text{adj } A)(B) = \begin{bmatrix} -4 & 8 & -4 \\ -1 & 2 & -1 \\ 3 & -6 & 3 \end{bmatrix} \begin{bmatrix} 3 \\ 6 \\ b \end{bmatrix} \neq O$$

$$\Rightarrow -12 + 48 - 4b \neq 0 \Rightarrow b \neq 9$$

Solution: 02

$$\text{The matrix equation is } \begin{bmatrix} k+1 & 8 \\ k & k+3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4k \\ 3k-1 \end{bmatrix}$$

For no solution of $AX = B$ a necessary condition is $\det A = 0$.

$$\Rightarrow \begin{vmatrix} k+1 & 8 \\ k & k+3 \end{vmatrix} = 0$$

$$\Rightarrow (k+1)(k+3) - 8k = 0 \Rightarrow k^2 + 4k + 3 - 8k = 0$$

$$\Rightarrow k^2 - 4k + 3 = 0 \Rightarrow (k-1)(k-3) = 0 \therefore k = 1, 3$$

For $k = 1$, the equation becomes

$$2x + 8y = 4, \quad x + 4y = 2$$

which is just a single equation in two variables, *i.e.*, $x + 4y = 2$ and it has infinite solutions.

For $k = 3$, the equation becomes

$$4x + 8y = 12, \quad 3x + 6y = 8$$

which are parallel lines. So no solution in this case

Solution: 03

Given system of equations is

$$x_1 + 2x_2 + x_3 = 3$$

$$2x_1 + 3x_2 + x_3 = 3$$

$$3x_1 + 5x_2 + 2x_3 = 1$$

It can be observed that the sum of first two equations yields

$$(x_1 + 2x_2 + x_3) + (2x_1 + 3x_2 + x_3) = 3 + 3$$

$$\Rightarrow 3x_1 + 5x_2 + 2x_3 = 6$$

But this contradicts the third equation, *i.e.*,

$$3x_1 + 5x_2 + 2x_3 = 1$$

So, the system is inconsistent and hence it has no solution.

Solution: 04

The given system of equations can be written as $AX = B$

For no solution $|A| = 0$ and $(\text{adj } A)(B) \neq O$

$$\text{Now, } |A| = 0$$

$$\Rightarrow \alpha^3 - 3\alpha + 2 = 0 \Rightarrow (\alpha - 1)^2(\alpha + 2) = 0$$

$$\Rightarrow \alpha = 1, -2$$

But for $\alpha = 1$, $|A| = 0$ and $(\text{adj } A)(B) = O$
 Also each equation becomes $x + y + z = 0$
 \Rightarrow for $\alpha = 1$ there exist infinitely many solution.
 Again for $\alpha = -2$
 $|A| = 0$ but $(\text{adj } A)(B) \neq O \Rightarrow \exists$ no solution

Solution: 05

The given system of equations is

$$(k+1)x + 8y = 0, \quad kx + (k+3)y = 0$$

Coefficient matrix, $A = \begin{bmatrix} k+1 & 8 \\ k & k+3 \end{bmatrix}$

$$\text{Now, } |A| = \begin{vmatrix} k+1 & 8 \\ k & k+3 \end{vmatrix} = (k+1)(k+3) - 8k$$

$$= k^2 + 4k + 3 - 8k = k^2 - 4k + 3 = (k-1)(k-3)$$

For unique solution $|A| \neq 0$ i.e., k must not be equal to 1 or 3.

Solution: 06

Let $A = \begin{bmatrix} 2 & 4 & -\lambda \\ 4 & \lambda & 2 \\ \lambda & 2 & 2 \end{bmatrix}$

For infinitely many solutions,

$$|A| = 0$$

$$\Rightarrow \begin{vmatrix} 2 & 4 & -\lambda \\ 4 & \lambda & 2 \\ \lambda & 2 & 2 \end{vmatrix} = 0$$

$$\Rightarrow 2(2\lambda - 4) - 4(8 - 2\lambda) - \lambda(8 - \lambda^2) = 0$$

$$\Rightarrow \lambda^3 + 4\lambda - 40 = 0$$

\therefore Number of values of $\lambda = 1$ ($\because \lambda(3) \cdot \lambda(4) < 0$)

Correct Options

Answer:01

Correct Options: D

Answer:02

Correct Options: A

Answer:03

Correct Options: D

Answer:04

Correct Options: B

Answer:05

Correct Options: D

Answer:06

Correct Options: B