A circular hole of radius $\frac{R}{4}$ is made in a thin uniform disc having mass M and radius R, as shown in figure.

The moment of inertia of the remaining portion of the disc about an axis passing through the point O and perpendicular to the plane of the disc is : [JEE MAIN (Online) 2017]



19MR²

512

(C)

197MR²

256

(B)



(D)
$$\frac{237MR^2}{512}$$

Let the mass per unit area of disc be Now, moment of inertia of removed mass

$$(\mathbf{M}_2) = \left(\frac{(\sigma \mathbf{A}')\left(\frac{\mathbf{R}}{4}\right)^2}{2} + (\sigma \mathbf{A}')\left(\frac{3\mathbf{R}}{4}\right)^2\right)$$

Using parallel axis theorem $M_2 = (\sigma A') \left(\frac{R^2}{32} + \frac{9R^2}{16} \right)$ $A' = \pi \left(\frac{R}{4} \right)^2 = \frac{\pi R^2}{16}$ $M_2 = \left(\frac{\sigma \pi R^4}{16} \right) \left(\frac{19}{32} \right)$

Also, moment of inertia of complete disc is:

 $\Rightarrow \mathbf{M}_1 = \left(\frac{(\sigma \mathbf{A}) \times \mathbf{R}^2}{2}\right)$

Effect moment of inertia = $M_1 - M_2$

$$M_{0} = \frac{\sigma}{2}\pi R^{4} - \frac{\sigma\pi R^{4}.19}{512}$$
$$M_{0} = (\sigma\pi R^{2}) .R^{2} .\frac{237}{512}$$
$$\sigma\pi R^{2} = M$$

$$M_0 = \frac{237}{512}MR^2$$