Find the wavelengths in a hydrogen spectrum between the range 500 nm to 700 nm.

olution : The energy of a photon of wavelength 500 nm is $\frac{hc}{\lambda} = \frac{1242 \text{ eV nm}}{500 \text{ nm}} = 2.44 \text{ eV}.$

The energy of a photon of wavelength 700 nm is

$$\frac{hc}{\lambda} = \frac{1242 \text{ eV nm}}{700 \text{ nm}} = 1.77 \text{ eV}.$$

The energy difference between the states involved in the transition should, therefore, be between 1.77 eV and 2.44 eV.



Figure 43-W1

Figure (43-W1) shows some of the energies of hydrogen states. It is clear that only those transitions which end at n = 2 may emit photons of energy between 1.77 eV and 2.44 eV. Out of these only $n = 3 \rightarrow n = 2$ falls in the proper range. The energy of the photon emitted in the transition n = 3 to n = 2 is $\Delta E = (3.4 - 1.5) \text{ eV}$ = 1.9 eV. The wavelength is

$$\lambda = \frac{hc}{\Delta E}$$
$$= \frac{1242 \text{ eV n m}}{1.9 \text{ eV}} = 654 \text{ nm}.$$