

Ques.

The temperature of an ideal gas in 3-dimensions is 300 K. The corresponding de-Broglie wavelength of the electron approximately at 300 K, is :

[m_e = mass of electron = 9×10^{-31} kg, h = Planck constant = $6.6 \times 6.6 \times 10^{-34}$ Js,

k_B = Boltzmann constant = 1.38×10^{-23} JK⁻¹]

Given, Planck's constant, $h = 6.6 \times 10^{-34}$ Js

Boltzmann constant, $k_B = 1.38 \times 10^{-23}$ J/K

Mass of an electron, $m_e = 9 \times 10^{-31}$ kg

Temperature of an ideal gas, $T = 300$ K

As we know that, de-Broglie wavelength,

$$\lambda = \frac{h}{mv} = \frac{h}{\sqrt{2mE}} \dots (i)$$

Here, E is the kinetic energy,

$$E = \frac{3k_B T}{2}$$

Substituting value of E in Eq. (i), we get

$$\lambda = \frac{h}{\sqrt{3m k_B T}}$$

Substituting the given values in the above equation, we get

$$\lambda = \frac{6.6 \times 10^{-34}}{\sqrt{3 \times 9 \times 10^{-31} \times 1.38 \times 10^{-23} \times 300}}$$

$$= 6.26 \text{ nm}$$

∴ The corresponding de-Broglie wavelength of an electron approximately at 300 K is 6.26 nm.