

⇒ Symmetric ~~and~~ Matrix $\Rightarrow A^T = A$
Skew symmetric matrix $\Rightarrow A^T = -A$

$$\Rightarrow (AB)^T = B^T A^T$$

$$(AB)^{-1} = B^{-1} A^{-1}$$

$$\text{adj}(AB) = \text{adj} B \cdot \text{adj} A$$

$$\Rightarrow (A^n)^T = (A^T)^n \quad (n \in \mathbb{N})$$

$$(A^n)^{-1} = (A^{-1})^n$$

$$\text{adj}(A^n) = (\text{adj} A)^n$$

$$\Rightarrow (A^T)^{-1} = (A^{-1})^T$$

$$\text{adj}(A^T) = (\text{adj} A)^T$$

$$\Rightarrow |A| = |A^T|$$

$$|A^n| = |A|^n$$

$$|AB| = |A| |B|$$

$$|A^{-1}| = \frac{1}{|A|}$$

$$\Rightarrow |\lambda A| = \lambda^n |A| \quad (n \rightarrow \text{order of matrix})$$

$$\Rightarrow \text{adj}(\lambda A) = \lambda^{n-1} \text{adj} A \quad (n \rightarrow \text{order of matrix})$$

$$(\lambda A)^{-1} = \frac{1}{\lambda} A^{-1}$$

$$\Rightarrow A \cdot \text{adj} A = |A| I = \text{adj} A \cdot A$$

$$\left\{ A^{-1} = \frac{\text{adj} A}{|A|}, (\text{adj} A)^{-1} = \frac{A}{|A|} \right\}$$

$$|\text{adj}(\text{adj}(\text{adj} \dots \text{adj} A))| = |A|^{(n-1)^k}$$

$n \rightarrow$ order of matrix
 k times

⇒ Any matrix 'A' can be represented as sum of a symmetric & skew symmetric matrix.

$$A = \underbrace{\frac{A+A'}{2}}_{\text{Symmetric}} + \underbrace{\frac{A-A'}{2}}_{\text{Skew-symmetric}}$$

⇒ Determinant of odd order skew symmetric matrix is zero.

⇒ If we interchange consecutive rows/columns in determinant, it is multiplied by -1 . If total 'm' 'consecutive rows/columns interchange' occur then determinant will be multiplied by $(-1)^m$.

Ex.

$$\begin{vmatrix} R_1 \\ R_2 \\ R_3 \end{vmatrix} \begin{matrix} \leftarrow \\ \leftarrow \end{matrix} = - \begin{vmatrix} R_2 \\ R_1 \\ R_3 \end{vmatrix} \begin{matrix} \leftarrow \\ \leftarrow \end{matrix} = (-1)^2 \begin{vmatrix} R_2 \\ R_3 \\ R_1 \end{vmatrix}$$
$$= \begin{vmatrix} R_2 \\ R_3 \\ R_1 \end{vmatrix}$$