

## FORMULAS TO REMEMBER:

- FOR SHM,  $F = -kx$   
or  $a = -\omega^2 x$       so,  $\omega = \sqrt{\frac{k}{m}}$
- EQUATION OF SHM -  $x = A \sin(\omega t + \phi)$        $\phi \equiv$  INITIAL PHASE
- Time Period  $\rightarrow T = \frac{2\pi}{\omega} = \frac{2\pi}{\sqrt{\frac{k}{m}}}$
- frequency  $\rightarrow f = \frac{1}{T} = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$
- $v = \frac{dx}{dt} = A\omega \cos(\omega t + \phi)$        $a = \frac{dv}{dt} = -A\omega^2 \sin(\omega t + \phi)$   
 $= -\omega^2 x$

## FORMULAS TO REMEMBER:

$$1 > v = \omega \sqrt{A^2 - x^2}, \quad a = -\omega^2 x$$

$$2 > \text{Kinetic Energy: } KE = \frac{1}{2} k (A^2 - x^2) = \frac{1}{2} k A^2 \cos^2(\omega t + \phi)$$

$$\text{Potential Energy: } PE = \frac{1}{2} k x^2 = \frac{1}{2} k A^2 \sin^2(\omega t + \phi)$$

$$\text{Total Energy: } TE = \frac{1}{2} k A^2 \rightarrow \text{constant.}$$

$$KE = PE = \frac{1}{4} k A^2 \quad \text{at } x = \pm \frac{A}{\sqrt{2}}$$

$$3 > \text{Diagram: Spring with mass } M \text{ and constant } k. \quad T = 2\pi \sqrt{\frac{M}{k}}, \quad v_{\max} = \omega A$$

$$4 > \text{Diagram: Vertical spring with mass } M. \quad T = 2\pi \sqrt{\frac{M}{k}}, \quad A = \frac{Mg}{k}$$

$$5 > \text{When spring has mass } M_s. \quad \text{Diagram: Spring with mass } M_s \text{ and mass } M. \quad T = 2\pi \sqrt{\frac{M + \frac{M_s}{3}}{k}}$$

• FORMULAS TO REMEMBER

1> for physical pendulum / rigid body oscillation

$$T = 2\pi \sqrt{\frac{I}{mg\ell}}$$

$I \equiv$  Moment of Inertia about point of suspension

$\ell \equiv$  Distance between COM and point of suspension.

2> for simple pendulum

$$T = 2\pi \sqrt{\frac{\ell}{g}}$$

when accelerated frame ( $\vec{a}$ )

use  $g = g_{\text{eff}} = |\vec{g} - \vec{a}|$