

Let n_1 and n_2 be the number of red and black balls respectively, in box I. Let n_3 and n_4 be the number of red and black balls, respectively, in box II. [esquestion]

Q. One of the two boxes, box I and box II, was selected at random and a ball was drawn randomly out of this box. The ball was found to be red. If the probability that this red ball was drawn from box II is $\frac{1}{3}$, then the correct option(s) with the possible values of n_1, n_2, n_3 and n_4 is (are) (A) $n_1 = 3, n_2 = 3, n_3 = 5, n_4 = 15$ (B) $n_1 = 3, n_2 = 6, n_3 = 10, n_4 = 50$ (C) $n_1 = 8, n_2 = 6, n_3 = 5, n_4 = 20$ (D) $n_1 = 6, n_2 = 12, n_3 = 5, n_4 = 20$

[JEE 2015, 4M, -0M]

Solution (a) Required probability = $\frac{\binom{n_3}{n_3+n_4}}{\frac{n_1}{n_1+n_2} + \frac{n_3}{n_3+n_4}} = \frac{1}{3}$ (now check option)

Q. All ball is drawn at random from box I and transfered to box II. If the probability of drawing a red ball from box I, after this transfer, is $\frac{1}{3}$, then the correct option(s) with the possible values of n_1 and n_2 is (are) (A) $n_1 = 4$ and $n_2 = 6$ (B) $n_1 = 2$ and $n_2 = 3$ (C) $n_1 = 10$ and $n_2 = 20$ (D) $n_1 = 3$ and $n_2 = 6$

[JEE 2015, 4M, -0M]

Solution (b) Required probability = $\frac{n_1}{n_1+n_2} \cdot \frac{n_1-1}{n_1+n_2-1} + \frac{n_2}{n_1+n_2} \cdot \frac{n_1}{n_1+n_2-1} = \frac{1}{3}$ (now check given option)

Q. A computer producing factory has only two plants T_1 and T_2 Plant T_1 produces 20% and plant T_2 produces 80% of the total computers J produced. 7% of computers produced in the factory turn out to be defective. It is known what

P (computer turns out to be defective given that is produced in plant T_1) =

$10P$ (computer turns out to be defective given that it is produced in plant T_2) where $P(E)$ denotes the probability of an event E . A computer produces in the factory is randomly eslected and it does not turn out to be defective. Then the probabality that it is produced plant T_2 is (A) $\frac{36}{73}$ (B)

$\frac{47}{79}$ (C) $\frac{78}{93}$ (D) $\frac{75}{83}$

[JEE(Advanced)-2016]

Solution :- $P(T_1) = \frac{20}{100}$ $P(T_2) = \frac{80}{100}$

Let $P\left(\frac{D}{T_2}\right) = x$ $P\left(\frac{D}{T_1}\right) = 10x$

$P(D) = \frac{7}{100}$ (given)

$P(T_1)P\left(\frac{D}{T_1}\right) + P(T_2)P\left(\frac{D}{T_2}\right) = \frac{7}{100}$

$\frac{20}{100} \times 10x + \frac{80}{100} \times x = \frac{7}{100} \quad \Rightarrow x = \frac{1}{40}$

$P\left(\frac{D}{T_2}\right) = \frac{1}{40} \quad \Rightarrow P\left(\frac{\bar{D}}{T_2}\right) = \frac{39}{40}$

$P\left(\frac{D}{T_1}\right) = \frac{10}{40} \quad \Rightarrow P\left(\frac{\bar{D}}{T_1}\right) = \frac{30}{40}$

$$P\left(\frac{T_2}{D}\right) = \frac{\frac{80}{100} \times \frac{39}{40}}{\frac{20}{100} \times \frac{30}{40} + \frac{80}{100} \times \frac{39}{40}}$$

$$= \frac{78}{93}$$

Football teams T_1 and T_2 have to play two games against each other. It is assumed that the outcomes of the two games are independent. The probabilities of T_1 winning, drawing and losing a game against T_2 are $\frac{1}{2}$, $\frac{1}{6}$ and $\frac{1}{3}$, respectively. Each team gets 3 points for a win, 1 point for a draw and 0 point for a loss in a game. Let X and Y denote the total points scored by teams T_1 and T_2 , respectively, after two games

Q. $P(X > Y)$ is- (A) $\frac{1}{4}$ (B) $\frac{5}{12}$ (C) $\frac{1}{2}$ (D) $\frac{7}{12}$

[JEE(Advanced)-2016]

Solution :- $P(X > Y) = P(T_1 \text{ win})P(T_1 \text{ win}) + P(T_1 \text{ win})P(\text{match draw}) + P(\text{match draw})P(T_1 \text{ win})$

$$= \frac{1}{2} \cdot \frac{1}{2} + \frac{1}{2} \cdot \frac{1}{6} + \frac{1}{2} \cdot \frac{1}{6} = \frac{1}{4} + \frac{2}{12} = \frac{1}{4} + \frac{1}{6} = \frac{10}{24} = \frac{5}{12}$$

Q. $P(X = Y)$ is- (A) $\frac{11}{36}$ (B) $\frac{1}{3}$ (C) $\frac{13}{36}$ (D) $\frac{1}{2}$

Solution :- $P(X = Y) = P(\text{match draw})P(\text{match draw}) + P(T_1 \text{ win})P(T_1 \text{ loss}) + P(T_1 \text{ loss})P(T_1 \text{ win})$

$$= \frac{1}{6} \cdot \frac{1}{6} + \frac{1}{2} \cdot \frac{1}{3} + \frac{1}{3} \cdot \frac{1}{2} = \frac{1}{36} + \frac{2}{6} = \frac{13}{36}$$

Q. Let X and Y be two events such that $P(X) = \frac{1}{3}$, $P(X|Y) = \frac{1}{2}$ and $P(Y|X) = \frac{2}{5}$. Then

(A) $P(X'|Y) = \frac{1}{2}$

(B) $P(X \cap Y) = \frac{1}{5}$

(C) $P(X \cup Y) = \frac{2}{5}$

(D) $P(Y) = \frac{4}{15}$

[JEE(Advanced)-2017]

$$\text{Solution: } P(X) = \frac{1}{3} \quad \frac{P(X \cap Y)}{P(Y)} = \frac{1}{2} \quad \frac{P(Y \cap X)}{P(X)} = \frac{2}{5}$$

$$P(X \cap Y) = \frac{2}{15} \quad P(Y) = \frac{4}{15}$$

$$P(X \cup Y) = P(X) + P(Y) - P(X \cap Y) = \frac{1}{3} + \frac{4}{15} - \frac{2}{15} = \frac{1}{3} + \frac{2}{15} = \frac{7}{15}$$

$$P(\bar{X} | Y) = \frac{P(\bar{X} \cap Y)}{P(Y)} = \frac{P(Y) - P(X \cap Y)}{P(Y)} = 1 - \frac{P(X \cap Y)}{P(Y)} = 1 - \frac{2/15}{4/15} = \frac{1}{2}$$